



INVESTIGATION OF DYNAMICS OF MANIPULATORS AND ROBOTS, THE MOTION OF WHICH IS EXCITED BY AN EXTERNAL VARIABLE FORCE THROUGH MUTUAL IMPACTS OF THEIR SEPARATE ELEMENTS

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Abstract

Manipulators and robots find a number of applications in agricultural engineering. They are used in pipe robots for transportation of materials. Also pipe robots are applied for cleaning of internal surfaces of the pipes. Impact interactions take place in the process of dynamic behavior in the elements of manipulators and robots. Their precise investigation is an important engineering problem. A model having one degree of freedom with forced excitation and impacts is investigated. The values of coefficient of restitution and coefficient of viscous damping have basic effect to the dynamic behavior of such systems. In this paper the investigations of the dependence of regions with single valued regimes of motion from the coefficient of restitution and from the coefficient of viscous damping are performed. This paper is devoted to numerical experiment: the model of the system is presented in detail as well as the parameters for which calculations were performed are indicated. The presented graphical relationships enable to choose the regimes suitable for operation of elements of manipulators and robots. They are applicable in the process of design of pipe robots.

Keywords: *elements of manipulators, elements of robots, impact interactions, forced excitation, nonlinear behaviour, coefficient of restitution, coefficient of viscous damping.*

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1. Introduction

Manipulators and robots find a number of applications in agricultural engineering. They are used in pipe robots for transportation of materials. Also pipe robots are applied for cleaning of internal surfaces of the pipes.

Impact interactions take place in the process of dynamic behavior in the elements of manipulators and robots. Their precise investigation is an important engineering problem.

Mechanical system of the manipulator – robot is presented in Fig. 1. The driving force of the case of the manipulator 1 is provided by the impacting element 2 to which the variable external force is acting, while the one-sided motion of the case 2 is ensured by the self stopping device 4 because of the interaction with the immovable foundation. The self stopping device may be a mechanism based on friction between the elements 4 and 5 or it can be based on mechanisms of various types, for example it can be a worm gear mechanism.

Pipe robot with impact interactions is described in (Spruogis *et al.*, 2002). In this paper impact interactions in the elements of a pipe robot are investigated in detail.

Pipe robots and their application in agricultural engineering are investigated in (Ragulskis, Spruogis, Bogdevičius, Pauliukas *et al.*, 2020). This paper continues the investigations about pipe robots in agricultural engineering presented in the previous paper.

Related problems of analysis of dynamics of nonlinear systems and elements of manipulators and robots are investigated in (Glazunov, 2018), (Blekhman, 2018), (Bolotnik *et al.*, 2016), (Bansevicius *et al.*, 1985), (Kibirkištis *et al.*, 2018), (Ragulskis *et al.*, 1965), (Mištinas *et al.*, 2006), (Ragulskis, Bogdevičius *et al.*, 2006), (Ragulskis, Spruogis, Matuliauskas, Mištinas, two references, 2006), (Matuliauskas *et al.*, 2007), (Ragulskis, Bogdevičius *et al.*, 2008), (Ragulskis, Ragulskis *et al.*, 2008), (Ragulskis, Spruogis, Bogdevičius, Matuliauskas, Mištinas, Ragulskis, three references, 2020), (Ragulskis, Spruogis, Bogdevičius *et al.*, 2021), (Ragulskis, Spruogis, Matuliauskas *et al.*, 2021), (Ragulskis, Spruogis, Paškevičius *et al.*, 2021), (Spedicato, Notarstefano, 2017), (Sumbatov, Yunin, 2013) and in a number of other research papers.

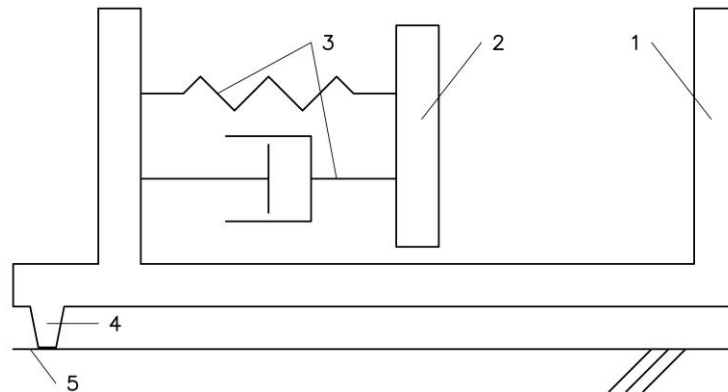


Fig. 1. Mechanical system of the manipulator – robot: 1 – case, 2 – element impacting into the case, 3 – elements connecting the impacting mass and the case, 4 – one sided self stopping device between the case and the immovable foundation, 5 – the immovable foundation

Dynamics of vibrating systems with impacts is investigated in (Ragulskienė, 1974). Transmissions and their vibrations are analysed in (Kurila, Ragulskienė, 1986). Dynamics of elements of manipulators and robots is presented in (Ragulskis *et al.*, 1987). This paper is based on some of the basic results presented in those three research monographs.

A model having one degree of freedom with forced excitation and impacts is investigated. The values of coefficient of restitution and coefficient of viscous damping have basic effect to the dynamic behavior of such systems. In this paper the investigations of the dependence of regions with single valued regimes of motion from the coefficient of restitution and from the coefficient of viscous damping are performed.

The presented graphical relationships enable to choose the regimes suitable for operation of elements of manipulators and robots. This paper is devoted to numerical experiment: the model of the system is presented in detail as well as the parameters for which calculations were performed are indicated. This paper is a continuation of investigations of the authors presented in their other papers.

The presented results of the performed investigation are used in the process of design of elements of manipulators and robots. They are applicable in the process of design of pipe robots.

2. Model of the element of the system with impact interactions

Dynamics of the investigated system in non dimensional form is described by the following differential equation:

$$x'' + 2hx' + x = f \sin v\tau, \quad (1)$$

where x denotes the non dimensional displacement, h denotes the non dimensional viscous damping coefficient, f denotes the non dimensional excitation amplitude, v denotes the non dimensional frequency, τ denotes the non dimensional time variable, the prime in the superscript indicates derivative with respect to non dimensional time.

This equation is valid when:

$$x < 0. \quad (2)$$

Impact is described in the following way:

$$x'^+ = -Rx'^-, \quad (3)$$

where R denotes the restitution coefficient, superscript minus denotes the quantity before impact, superscript plus denotes the quantity after impact.

Impact takes place when:

$$x = 0. \quad (4)$$

Zero initial conditions were assumed, that is:

$$x(0) = 0, \quad x'(0) = 0. \quad (5)$$

Motions of the investigated element of manipulators and robots in regimes that are periodic are analysed.

3. Dependence of regions of single valued motions of the investigated element of manipulators and robots from the coefficient of restitution

The following values of the parameters of the vibro impact system with forced excitation were assumed in the presented investigation:

$$f = -0.5, \quad h = 0.1. \quad (6)$$

3.1. Regions in the vicinity of the value of non dimensional frequency equal to two

Main characteristics of dynamics of the investigated system in periodic regime of motion at $\nu = 2$ are shown in Fig. 2.

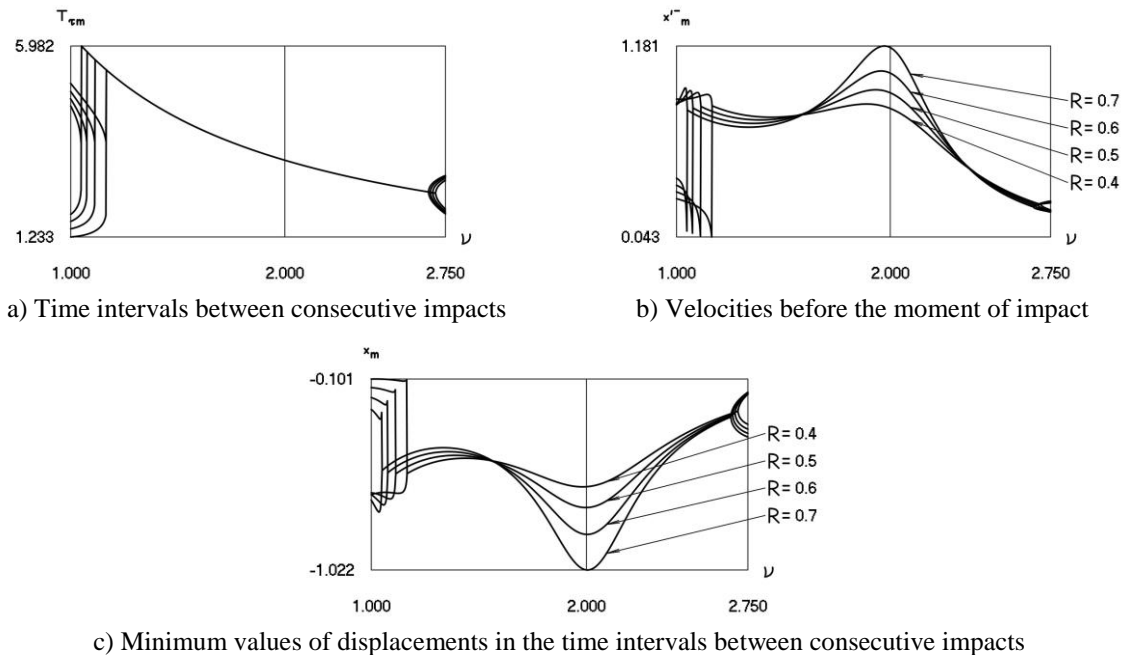


Fig. 2. Dependence of minimum values and of maximum values from the coefficient of restitution for $f = -0.5, h = 0.1$ in the vicinity of $\nu = 2$

In Fig. 2 the values of time intervals between consecutive impacts, velocities before the moment of impact and minimum values of displacements in the time intervals between consecutive impacts are represented. Results for the following values of coefficient of restitution $R=0.4, R=0.5, R=0.6, R=0.7$ are presented. Time intervals between consecutive impacts are mutually similar in a greater part of the represented frequency region for the four values of coefficient of restitution. Frequency regions with single valued regimes of motion and their dependence on the coefficient of restitution are seen from the presented graphical relationships.

3.2. Regions in the vicinity of the value of non dimensional frequency equal to four

Main characteristics of dynamics of the investigated system in periodic regime of motion at $\nu = 4$ are shown in Fig. 3.

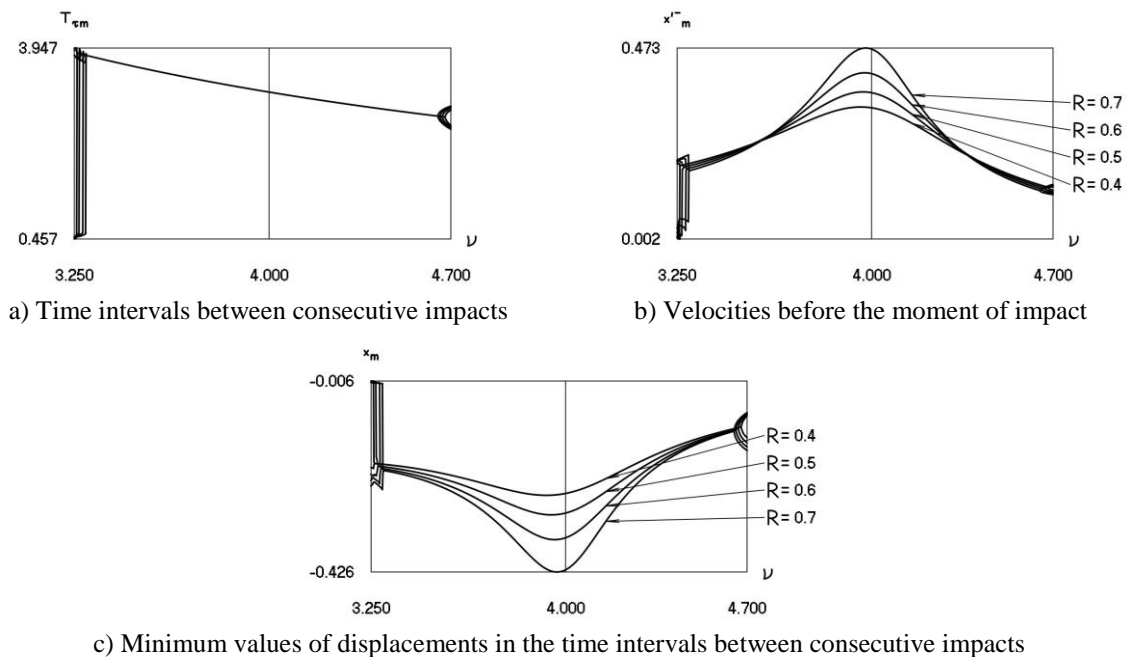


Fig. 3. Dependence of minimum values and of maximum values from the coefficient of restitution for $f = -0.5, h = 0.1$ in the vicinity of $\nu = 4$

3.3. Regions in the vicinity of the value of non dimensional frequency equal to six

Main characteristics of dynamics of the investigated system in periodic regime of motion at $\nu = 6$ are shown in Fig. 4.

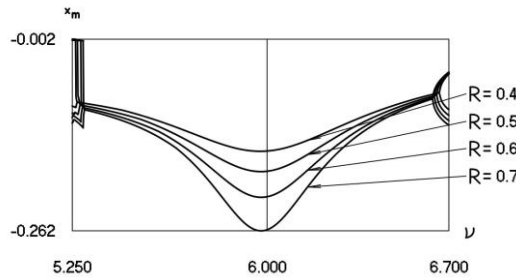
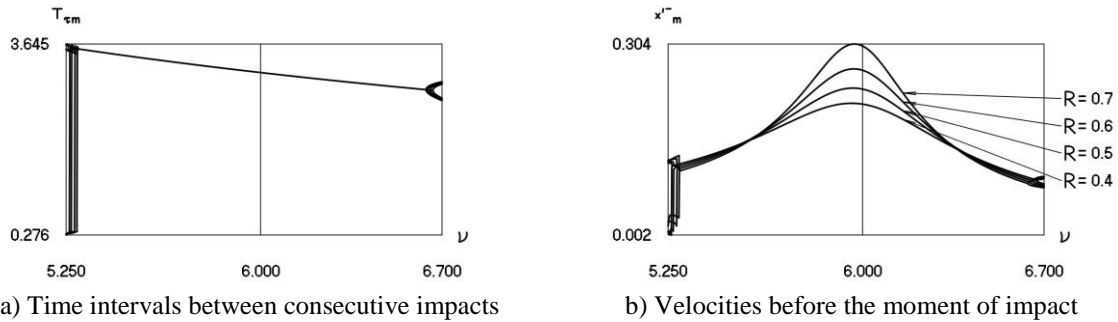
4. Dependence of regions of single valued motions of the investigated element of manipulators and robots from the coefficient of viscous damping

The following values of the parameters of the vibro impact system with forced excitation were assumed in the presented investigation:

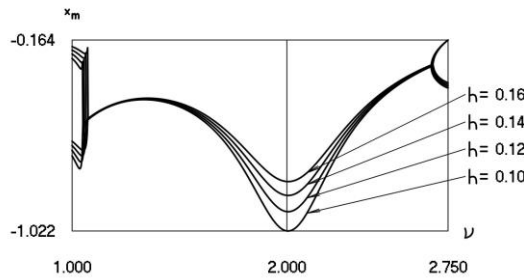
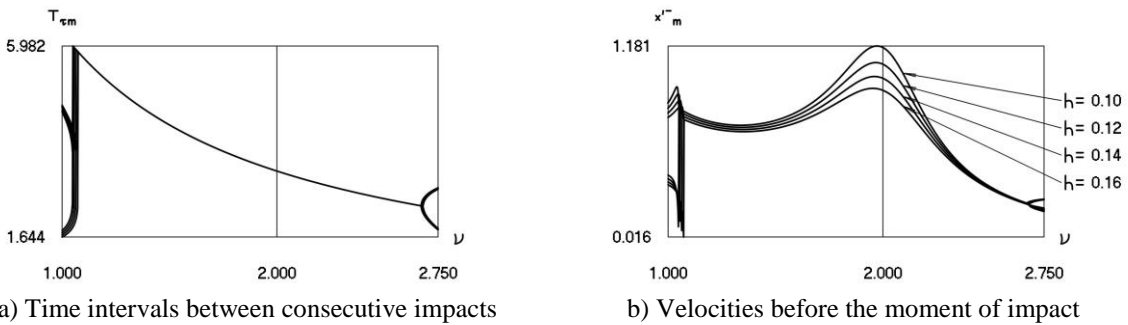
$$f = -0.5, R = 0.7. \quad (7)$$

4.1. Regions in the vicinity of the value of non dimensional frequency equal to two

Main characteristics of dynamics of the investigated system in periodic regime of motion at $\nu = 2$ are shown in Fig. 5.



c) Minimum values of displacements in the time intervals between consecutive impacts
Fig. 4. Dependence of minimum values and of maximum values from the coefficient of restitution for $f = -0.5, h = 0.1$ in the vicinity of $\nu = 6$



c) Minimum values of displacements in the time intervals between consecutive impacts
Fig. 5. Dependence of minimum values and of maximum values from the coefficient of viscous damping for $f = -0.5, R = 0.7$ in the vicinity of $\nu = 2$

In Fig. 5 the values of time intervals between consecutive impacts, velocities before the moment of impact and minimum values of displacements in the time intervals between consecutive impacts are represented. Results for the following values of coefficient of viscous damping $h = 0.1, h = 0.12, h = 0.14, h = 0.16$ are presented. Time intervals between consecutive impacts are mutually similar in a greater part of the represented frequency region for the four values of coefficient of viscous damping. Frequency regions with single valued regimes of motion and their dependence on the coefficient of viscous damping are seen from the presented graphical relationships.

4.2. Regions in the vicinity of the value of non dimensional frequency equal to four

Main characteristics of dynamics of the investigated system in periodic regime of motion at $\nu = 4$ are shown in Fig. 6.

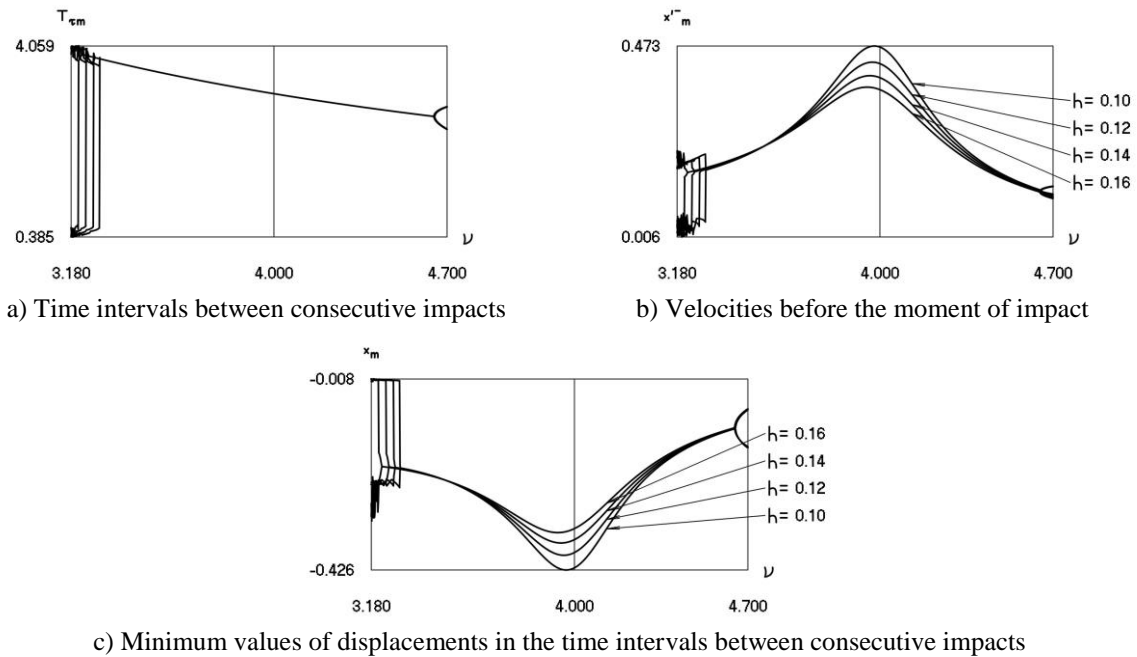


Fig. 6. Dependence of minimum values and of maximum values from the coefficient of viscous damping for $f = -0.5$, $R = 0.7$ in the vicinity of $\nu = 4$

4.3. Regions in the vicinity of the value of non dimensional frequency equal to six

Main characteristics of dynamics of the investigated system in periodic regime of motion at $\nu = 6$ are shown in Fig. 7.

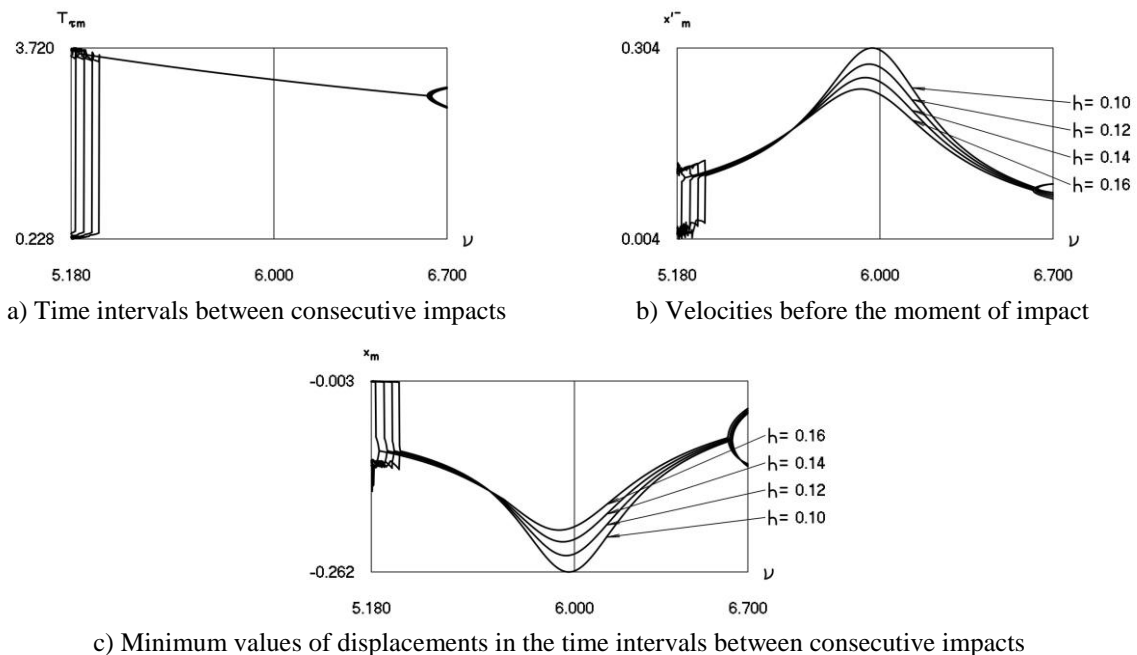


Fig. 7. Dependence of minimum values and of maximum values from the coefficient of viscous damping for $f = -0.5$, $R = 0.7$ in the vicinity of $\nu = 6$

5. Conclusions

Impact interactions take place in the elements of manipulators and robots, especially in pipe robots, which are used in agricultural engineering.

In this paper a model having one degree of freedom with forced excitation and impacts is investigated numerically. Such impact interactions take place in the elements of pipe robots. The values of coefficient of restitution and coefficient of viscous damping have basic effect to the dynamic behavior of such systems.

Various dynamic regimes of operation in essentially nonlinear systems, such as vibro impact systems, take place. They include multi valued and chaotic regimes of motion. Regions of single valued motions play an important role in the theory of vibro impact systems, as they are desirable from the engineering point of view. Thus, the investigations of the dependence of regions with single valued regimes of motion from the coefficient of restitution and from the coefficient of viscous damping are performed.

The presented graphical relationships enable to choose the regimes suitable for operation of elements of manipulators and robots, including pipe robots, which are applicable in agricultural engineering. The three obtained regions of single valued motions and their dependence on the coefficient of restitution and on the coefficient of viscous damping are described in detail: in the vicinity of the value of non dimensional frequency equal to two, in the vicinity of the value of non dimensional frequency equal to four and in the vicinity of the value of non dimensional frequency equal to six.

This paper is devoted to numerical experiment: the model of the system is presented in detail as well as the parameters for which calculations were performed are indicated.

The presented results of the performed investigation are used in the process of design of elements of pipe robots in which impact interactions take place.

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